

# Research on Audit Index System of "Special Bonds + PPP" Based on FAHP

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## Abstract

This paper starts from the angle of life-cycle audit coverage, and builds the whole-process audit index system of the "special bonds + PPP" public infrastructure construction model project (hereinafter referred to as "special bonds + PPP"). Firstly, through literature research and interviews with institutional experts, the audit index system is built in accordance with the three dimensions: including early project approval decision, medium-term administration as well as later handover evaluation; secondly, the fuzzy analytic hierarchy process(FAHP) is introduced to sequence and assign values to various indexes, and build judgment matrices; In the end, on the basis of the questionnaire information data of importance order of evaluation index system filled in by experts, the weight value is calculated with the MATLAB program; It makes the audit index system scientific and operable.

## Keywords

Special bonds + PPP; Audit index; FAHP.

## 1. Introduction

Public-Private Partnership (PPP) has been fully applied to China's infrastructure construction since 2014, in order to resolve the defect of the increasingly prominent financing difficulties, local governments have issued special bonds in combination with projects, the "special bond + PPP" public infrastructure construction model project (hereinafter referred to as "special bond + PPP") has become an important promoter of our country's infrastructure construction. At present, there are few theoretical research results in "special bonds + PPP" whole-process tracking audit index system, practical results lack systematic summary, audit development lacks scientific basis; a scientific and fitting audit index system need to be built to make audit work well-founded, and this has important implications to ensure the operating legality of such projects and achieve the expected benefits.

## 2. Building of the Whole-Process Tracking Audit Index System of "Special Bonds + PPP"

### 2.1. Audit Dimensions and Key Identification of PPP Project

PPP projects have the characteristics of long cooperation period, numerous participating subjects and different interests and appeals of all parties, scholars have done extensive research on the identification of reasonable and effective audit dimensions and audit priorities. This paper analyzes the audit dimensions and key identification established by various scholars based on literature research, as shown in Table 1.

**Table 1. Research on audit dimensions and key identification of PPP project**

scholar	audit dimension	identification of audit priorities
Yan Xiaojian [1]	(1) results and benefits (2) execution process	(1) products and services; (2) public satisfaction; (3) bidding procedures; (4) contract management; (5) risk allocation; (6) performance evaluation; (7) audit environment
Lu Xinyi[2]	(1) early project approval (2) medium-term construction (3) later assessment	(1) project screening; (2) feasibility report; (3) contract terms of franchise; (4) project design; (5) assessment and argument; (6) cooperation way; (7) commercial contracts; (8) risk share; (9) project quality; (10) capital estimation
Shi Xian[3]	(1) project cost (2) project management (3) investment performance	(1) investment estimation; (2) design estimation; (3) partner selection methods and procedures; (4) cooperation contracts; (5) quality and progress management; (6) budget and final account execution; (7) project construction procedures ; (8) bid procedures; (9) contract management; (10) risk management; (11) economic benefits; (12) construction effects; (13) public service capability
Wang Ligu, Zhang Ying[4]	(1) policy implementation (2) project approval (3) process operation (4) investment performance	(1) policy implementation; (2) institutional measure; (3) policy strategy system; (4) feasibility study; (5) construction procedures; (6) bid; (7) quality and progress management; (8) environmental protection; (9) budget and final accounts execution; (10) mechanism construction; (11) management effect; (12) financial performance; (13) comprehensive benefits
Fang Jun, Ren Suping, Huang Juntian[5]	(1) project approval decision (2) administration (3) handover evaluation	(1) project development procedures; (2) relevant procedures and documents; (3) applicability of models; (4) governmental investment decisions; (5) governmental administration functions; (6) project financing; (7) fund management and use; (8) project handover procedure; (9) evaluation of good value for money
Zhao Chong, Gao Yun[6]	(1) project decision (2) project implementation (3) project operation and maintenance	(1) approval procedure; (2) feasibility study report; (3) environmental assessment; (4) demolition assessment; (5) bid procedure; (6) project design; (7) quality and progress management; (8) funds management; (9) contract management; (10) project settlement; (11) economic benefits; (12) social benefits; (13) environmental benefits
Ye Xiaosu, Zhang Deqin, Shi Shiyong[7]	(1) audit main body (2) audit time sequence (3) audit execution	(1) project planning and approval; (2) franchise; (3) risk allocation; (4) financing risk; (5) governmental gap fund subsidy; (6) pricing standard/user charges; (7) total project cost (tpc); (8) bid; (9) project construction procedures; (10) supervision of project construction activities; (11) commercial development; (12) operation, maintenance, development and revenue; (13) good value for money (3e); (14) pv; (15) asset valuation
Huang Wanyi, Lu Yongsong[8]	(1) project identification (2) project preparation (3) project purchase (4) project execution (5) project handover	(1) identification process; (2) investment estimation; (3) good value for money; (4) financial affordability argument; (5) implementation plan; (6) contract system; (7) organizational structure; (8) operation cost; (9) investment return mechanism; (10) approval process; (11) bid procedure; (12) financing plan; (13) construction management; (14) asset evaluation; (15) performance testing; (16) performance evaluation
Sun Lingzhi, Jia Hongjun, Ren Renxin[9]	(1) implementation process (2) management elements (3) participating body	(1) feasibility study report; (2) approval documents; (3) approval process; (4) environmental assessment; (5) undertaker selection; (6) bid procedure; (7) project design; (8) investment control; (9) quality and progress management; (10) contract management; (11) good value for money; (12) functional evaluation; (13) operational costs; (14) organizational structure
Jiao Sheng[10]	(1) project identification (2) project preparation (3) project purchase (4) project execution (5) project handover	(1) project initiation and screening; (2) approval process; (3) good value for money; (4) financial affordability; (5) environmental impact assessment; (6) feasibility study report; (7) evaluation of good value for money (8) bidding procedures; (9) contract management; (10) quality and progress management; (11) project construction cost; (12) performance evaluation; (13) asset value assessment

## 2.2. Key Identification of Special Bonds

The government issues special bonds for public infrastructure construction projects of the PPP mode, takes advantage of the short issuance cycle and low financing interest rate of special bonds, thereby improving the performance of PPP projects. After the introduction of special bonds, the financing model and implementation process of PPP projects have changed, and new

audit priorities should be added. This paper summarizes the audit priorities of special bond through literature review and interviews with institutional experts, as shown in Table 2.

**Table 2.** Research on key identification of special bonds

scholar or institution	identification of audit priorities
Wen Laicheng, Diao Weitao, Chen Baodong[11]	(1) use progress of funds; (2) intensity of information disclosure; (3) investment direction and use of funds
Chai Yunlong[12]	(1) issuance ways; (2) issuance life; (3) repay capital with interest
Xu Bo, Yang Wei[13]	(1) rights and liabilities of the issuer; (2) scale and structure; (3) project selection; (4) utilization efficiency of funds; (5) source of debt paying funds
Wangqing County Audit Bureau	(1) bond raising; (2) bond distribution; (3) bond release; (4) bond issuance; (5) bond management and use
21st Century Business Herald	(1) utilization rate of special bond funds; (2) investment direction of special bond funds; (3) solvency of principal and interest of debt
Liang Jiang New Area Audit Bureau	(1) whether the investment direction of bond funds is accurate; (2) whether the use of bond funds is standard; (3) whether the use of bond funds is efficient
Qingdao Chengyang District Audit Bureau	(1) bond borrowing; (2) bond use; (3) bond repayment; (4) responsibility monitoring

### 2.3. Building Principles of Index System

(1) Quantitative and qualitative principle, the introduction of qualitative index can prevent audit from only being superficial on the data, and the combination of quantitative index can effectively avoid the excessive influence of subjective factors.

(2) Layering principle. After the PPP project is combined with the special bonds, the number of participating main body and audit priorities increase, the method of layering construction is adopted to identify the audit priorities, and the indexes are layered to make the layers clear and easy to evaluate.

(3) Crucial and overall principle, the short-term benefits and long-term benefits of PPP projects are combined, the importance and relevance of indexes are fully considered, avoid the important and dwell on the trivial, and reduce the difficulty within a reasonable range.

(4) Scientific and operable principle, the indexes are scientifically set, in order to achieve the effect of full coverage and operability, and help the collection and analysis of evaluation results.

### 2.4. Building of Index System

According to the research and analysis of Table.1 and Table.2, it is found that the current PPP project audit dimensions are divided into the following kinds: firstly, according to the full life cycle theory of the project, they are divided into audit of early project approval decision stage, audit of medium-term administration stage, and audit of the later handover evaluation stage; secondly, according to the work flow, they are divided into five stages: project identification, preparation, purchase, execution, and handover; thirdly, according to the key points of project management and control, they are divided into the implementation process, management elements, and participating main body, all of which starts from the audit idea before, during and after the event. Combining the audit priorities proposed by the above experts and scholars based on different dimensions and perspectives, in order to achieve full coverage of audit and

fit the actual process of project application and use, and follow the building principle of index, this paper extracts the specific indexes of the whole-process tracking audit of "special bonds + PPP" in accordance with the three dimensions: early project approval decision, middle-term administration and later handover evaluation, it builds the whole-process tracking audit index system including 3 first-level indexes (represented by P), 23 second-level indexes (represented by S), and 68 third-level indexes (represented by T). The specific index names and index connotations are shown in Table 3.

**Table 3.** The whole-process tracking audit index system of "special bonds + PPP"

first-level index	second-level index	third-level index	index connotation
early project approval decision P <sub>1</sub>	project identification procedure S <sub>1</sub>	project initiation, screening procedure T <sub>1</sub>	according to the Ministry of Finance's No.76 document [2014] and relevant laws and regulations, evaluate the legality of procedure
		complete procedures and documents T <sub>2</sub>	compliant approval procedures, complete and correct documents
	investment estimation S <sub>2</sub>	approval procedure T <sub>3</sub>	according to the "Administrative Measures of the Franchise of Infrastructure and Public Utilities" issued by the National Development and Reform Commission [2014] No. 2724, evaluate the compliance of approval procedure
		evaluation procedure T <sub>4</sub>	open and transparent project evaluation procedure
		compilation basis T <sub>5</sub>	the compilation basis for investment estimation is correct, reasonable and sufficient, and should be combined with the project proposal and the final account data of the completion of similar projects
		estimation accuracy T <sub>6</sub>	the accuracy of investment estimation, rationality of errors
	preliminary implementation plan S <sub>3</sub>	compilation basis for plan T <sub>7</sub>	the correctness of plan compilation basis should include relevant laws, regulations and documents in the fields of purchase, investment and financing, PPP and special bonds, etc.
		signing of franchise contract T <sub>8</sub>	according to No. 25 document of Six Ministries and Commissions "Administrative Measures for Franchise of Infrastructure and Public Utilities", evaluate the compliance, legality and practicality of the terms of the contract
		cooperation way T <sub>9</sub>	the rationality of project cooperation way, compliance degree with actual situation of project
		contract system T <sub>10</sub>	according to the relevant provisions of the "Contract Law", evaluate the integrity of the commercial contract system, and the clarity of the assignment main body and core terms, etc.
	return on investment mechanism T <sub>11</sub>	the correctness of calculation method of governmental payment or feasibility gap subsidy, the rationality of the return source and payment mechanism, the legality, compliance and flexibility of the incentive mechanism	
	good value for money report S <sub>4</sub>	good value for money report T <sub>12</sub>	the integrity of good value for money report should cover seven major contents, namely project survey, background, significance, operation mode; definition of good value for money, qualitative and quantitative analysis and evaluation; attached list.
		qualitative analysis content T <sub>13</sub>	the pertinence of qualitative analysis of good value for money, including the discussion of the proposed PPP project from the aspects of increasing public supply, optimizing risk allocation, financing, and feasibility during the concession period, etc.
		quantitative calculation T <sub>14</sub>	the correctness of quantitative calculation, including PSC value, PPPs value and annual discount rate calculation
		annual discount rate T <sub>15</sub>	the accuracy of the annual discount rate is determined based on the Ministry of Finance's No.113 document [2014] and the local financial subsidy expenditure year basis and refer to the return of local government bonds in the same period
	financial affordability argument S <sub>5</sub>	argument report T <sub>16</sub>	the integrity of the general financial affordability evaluation report should include six parts, namely project survey, implementation significance, operation mode, governmental financial situation analysis, responsibility identification of governmental project, and assessment of governmental financial capacity
		relevant calculation T <sub>17</sub>	the accuracy of relevant calculation, including the reasonable profit rate of social capital, annual operating costs, governmental operating subsidy expenditure, and general public budget expenditure
		responsibility identification of financial expenditure T <sub>18</sub>	the responsibility identification rationality of financial expenditure
	risk sharing S <sub>6</sub>	risk balance configuration T <sub>19</sub>	the rationality of basic framework of risk allocation

middle-term administrationP <sub>2</sub>		combination of governmental resources and social capital T <sub>20</sub>	review the effectiveness of combination of governmental resources and social capital
		get governmental support T <sub>21</sub>	according to [2014] No. 2724 "Administrative Measures of Franchise of Infrastructure and Public Utilities", evaluate the compliance of the project's practical operation and whether it has excessively obtained governmental support
	purchase procedure S <sub>7</sub>	purchase document T <sub>22</sub>	the integrity of the purchase document compilation, contents should include purchase invitations, instructions to bidders, PPP project contract (draft), project purchase requirements, evaluation methods, format of bidding documents, qualification documents, and project implementation plans proposed by bidders, etc.
		transparency of information disclosure T <sub>23</sub>	the timeliness and transparency of relevant information disclosure and announcement in the purchase procedure
		response document review T <sub>24</sub>	according to the "Government Purchase Law of the People's Republic of China" and "Bid Law of the People's Republic of China", evaluate and review legality and compliance
		contract signing T <sub>25</sub>	the legality of the contract signing procedure, the integrity of the terms and the consistency of the bid document
	application procedure of special bonds S <sub>8</sub>	application procedure T <sub>26</sub>	according to the "Interim Measures of the Issuance Administration of Special Bonds of Local Governments", evaluate the integrity of the application procedure
		budget compilation T <sub>27</sub>	according to the relevant provisions of the Ministry of Finance's "Administrative Measures of Budgets of Special Debt of Local Governments" No.155 [2016], evaluate the rationality of budget compilation
		bond accounting T <sub>28</sub>	according to "Views on Strengthening the Management of Local Government Debts" (the State Council [2014] No. 43) and "Administrative Measures of the Budget Management of Special Bonds of Local Governments in 2015" (the Ministry of Finance [2015] No. 32), evaluate the accounting accuracy of special bonds
	project income solvency S <sub>9</sub>	balance receipts and payment capacity T <sub>29</sub>	project income and financing are balance
		solvency analysis T <sub>30</sub>	combining the special income and government gap subsidy repayment during the operation period, evaluate the accuracy of the solvency calculation and the correctness of the governmental understanding of the solvency
	fulfilment of governmental administrative functions S <sub>10</sub>	government administration T <sub>31</sub>	effective administration of project construction and operation of the government, financial departments and industry authorities
		administration of special bond funds T <sub>32</sub>	effectiveness, timeliness and risk prevention capacity of administration of special bond funds
		legal attainments of staff T <sub>33</sub>	familiarity of government departments, industry bodies, project leaders, auditors and finance professionals with policies and regulations of special bonds
rationality of project financing S <sub>11</sub>	financing structure T <sub>34</sub>	according to the "Implementation Views on Promoting the Standardized Development of Cooperation between Government and Social Capital" (the Ministry of Finance [2019] No.10), evaluate the rationality of the financing structure.	
	financing plan T <sub>35</sub>	the economy of financing plans includes the comparison of various plans and the correctness of plan compilation	
	calculation results T <sub>36</sub>	calculation accuracy related to financing plan	
use rationality of special bonds S <sub>12</sub>	idle rate of funds T <sub>37</sub>	whether the special bonds are idle, the funds are useless, and the interest is paid in vain	
	connection between funds and project T <sub>38</sub>	the connection condition between the application and use of special funds and the progress of the project, ensures that the bond funds are issued, used and effective as soon as possible	
	return period and bond period T <sub>39</sub>	the matching degree between the project income period and the bond period should meet the conditions that the project income period covers the bond period, and guarantee the solvency condition of the project	
	fund information T <sub>40</sub>	all information in the use of special funds is open and transparent	
legality of construction procedure S <sub>13</sub>	plan decision T <sub>41</sub>	the rationality of project plan and decision, take into account the quality, cost and construction period	
	construction procedure T <sub>42</sub>	according to the relevant documents of the Ministry of Finance and the National Development and Reform Commission on the implementation of the PPP model, evaluate the perfection and compliance of the construction procedures	
fulfilment degree of project company S <sub>14</sub>	cooperation agreement T <sub>43</sub>	the execution degree of cooperation agreement, including the consistency between the results achieved by the project at various stages of construction and operation and the expected goals	

later handover evaluation P <sub>3</sub>	evaluation quality of middle-term performance S <sub>15</sub>	quality safety and progress management T <sub>44</sub>	the quality of construction and operation, the deviation degree of the construction progress in comparison with the expected plan, and the reliability of the actual quality of the project
		project cost T <sub>45</sub>	reduction rate of project cost = (incurred cost of current PPP project - incurred cost of current similar traditional project) / incurred cost of current similar traditional project
	evaluation quality of middle-term performance S <sub>15</sub>	performance system T <sub>46</sub>	review the rationality of the performance system, the evaluation index system should be built in accordance with the evaluated objectives
		incentive effect of plan T <sub>47</sub>	whether the compiled incentive plan can achieve the expected incentive goals
	payment condition of project completion S <sub>16</sub>	settlement price T <sub>48</sub>	the settlement price is reasonable and consistent with the contract or market price
		completion settlement T <sub>49</sub>	correctness of completion settlement compilation, including compilation basis, project quantity change, claim, other inspection and calculation correctness
		final account compilation of completion T <sub>50</sub>	the final account rationality of completion, including the compilation basis and the correctness of the contents of the final accounts
	gap subsidy condition of government feasibility S <sub>17</sub>	pricing and subsidies T <sub>51</sub>	pricing rationality of operating income, including subsidies in line with actual conditions and contract agreements
		subsidy funds T <sub>52</sub>	the calculated correctness of subsidy funds, gap subsidy of government feasibility = availability return annuity + operation and maintenance return of the year - user fee income of the year
	financial and operational situation S <sub>18</sub>	account book, accounting statement T <sub>53</sub>	the authenticity and effectiveness of the account book and accounting statement, including the authenticity of the accounts and the compilation correctness of the cash flow statement
		project operation T <sub>54</sub>	openness and transparency of various businesses and operating income during the project operation period
		user fee T <sub>55</sub>	the rationality of fee standard, including practicality, reasonable pricing, and compliance in the operation process
	compliance of project handover S <sub>19</sub>	handover procedure T <sub>56</sub>	procedure compliance, including integrity of handover object, legal transfer and management rights
		handover content T <sub>57</sub>	content integrity, including that the handover content meets the terms of the contract.
		achievement rate of handover standard T <sub>58</sub>	the standard achievement rate, including the equipment integrity rate, the shortest service life, and deviation degree set by other indexes
	economy of handover subsidy amount S <sub>20</sub>	asset evaluation procedure T <sub>59</sub>	asset evaluation procedure is in place and legal
		asset evaluation plan T <sub>60</sub>	the asset evaluation plan include that the transfer working group and the social capital confirm the transfer situation and compensation method, and the rationality and pertinence of the asset evaluation plan
	effectiveness of performance test S <sub>21</sub>	performance test program T <sub>61</sub>	overall normativeness of performance test program
performance test plan T <sub>62</sub>		the performance test plan includes the feature pertinence and rationality of the project to be handed over	
repayment degree of principal and interest of special bonds S <sub>22</sub>	repayment rate of principal and interest T <sub>63</sub>	repayment of principal and interest of special bonds, repayment rate = principal and interest repaid / principal and interest to be repaid	
	repayment coverage rate of special income T <sub>64</sub>	whether the special income fully covers the repayment of the principal and interest of the special bonds, achieve return self-balance, and whether the special operating income repays the principal and interest of the special bonds in time	
rationality final performance evaluation S <sub>23</sub>	public goods or service efficiency T <sub>65</sub>	the fulfilment condition of the functions of the "special bonds + PPP" project, and the efficiency and practicality of the public products or services provided	
	public satisfaction T <sub>66</sub>	the public satisfaction with project outcome	
	environmental impact rate T <sub>67</sub>	the degree of environmental impact on society, economy and ecology after the project is completed	
	reduction rate of project investment T <sub>68</sub>	the construction economy of final investment of the project in comparison with the traditional modes	

### 3. Weight Determination of the Whole-Process Tracking Audit Index System of "Special Bonds + PPP"

#### 3.1. Determination of the Weight Calculation Method

Each index in the index system built above has a different impact on the project, for scientific evaluation, the weight of each index needs to be determined. At present, the weight determination methods mainly include subjective weighting method, objective weighting

method and subjective and objective comprehensive integrated weighting method. After fully studying the advantages and disadvantages of various weighting methods, combining the features of "special bonds + PPP" and the conditions at this stage, this paper initially considers using the analytic hierarchy process (AHP) to calculate the weight. AHP can quantify the qualitative judgments made by decision makers based on subjective experience, which not only fully considers experts' experience and avoids being separated from reality, but also quantifies the decision process and avoids subjective arbitrariness and AHP can complete the determination of weights without huge sample data. However, the traditional AHP requires experts to make "comparison in pairs" on indexes, in the case of a large number of audit indexes in this paper, repeated "comparison in pairs" will easily affect the consistency of experts' thinking, thereby affecting the accuracy of the final judgment results. In order to avoid the defects caused by AHP, finally, this paper decided to introduce the improved AHP, changed the "comparison in pairs" to order assignment, namely the fuzzy analytic hierarchy process (FAHP), which optimized based on retaining the advantages of traditional methods, and effectively improved the efficiency and capacity of AHP to solve problems.

### 3.2. Building of FAHP Model

#### (1) Building of hierarchical structure model

A hierarchical structure model is built, and complex problems are decomposed into factors with logical relationships through the model, and the lower layer of factors is the subdivision of the upper layer of factors.

#### (2) Factor sorting and assignment

Expertise is used to sort the factors in the hierarchical structure, assign the most important factor as 10, the least influential factor as 1, and the other factor assignments are calculated as follows:

$$u_k = 1 + \frac{10-1}{n-1}(k-1)$$

In the formula:  $k$  is the serial number of the influencing factors after the influencing factors are sorted in ascending order by severity;  $u_k$  is the value assigned to  $k$ -th factor;  $n$  is the number of influencing factors,  $n \geq 2$ .

#### (3) Building of the judgment matrix

The positive and negative judgment matrix  $A(A = (a_{ij})_{n \times n})$  is built, and the element  $a_{ij}$  of the matrix take the value in accordance with the following formula.

$$a_{ij} = \left\{ \begin{array}{l} u_i - u_j, u_i - u_j > 0 \\ 1, u_i - u_j = 0 \\ \frac{1}{|u_i - u_j|}, u_i - u_j < 0 \end{array} \right\}$$

In the formula:  $a_{ij}$  is the elements of the judgment matrix,  $u_i$  and  $u_j$  are the assignments of the factors  $i$  and  $j$ ,  $i, j = 1, 2, \dots, n$ .  $a_{ij}$  has the following properties: (1)  $0 < a_{ij} < 1$ ; (2)  $a_{ij} \cdot a_{ji} = 1$ ; (3)  $a_{ii} = 1$ ; thus building the following judgment matrix  $A$ .



$$A = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \cdots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{bmatrix}$$

#### (4) Calculation of Weights

1) Column vector normalization, namely, normalize each column of the judgment matrix.

$$a'_{ij} = \frac{a_{ij}}{\sum_{j=1}^n a_{ij}}$$

In the formula:  $a'_{ij}$  ——the matrix element obtained after the column vector is normalized.  
 $i, j = 1, 2, \dots, n$ .

2) Each row of vector after normalization is added up to get the column vector  $a$ ,

$$a_i = \sum_{j=1}^n a'_{ij} ; a = (a_1, a_2, \dots, a_n)^T$$

In the formula:  $a'_i$  is the value after the addition of  $i$ -th row,  $i, j = 1, 2, \dots, n$ ;

3) After the vector  $a$  is normalized, the matrix eigenvector  $W$  is obtained

$$w_i = \frac{a_i}{\sum_{i=1}^n a_i} ; W = (w_1, w_2, \dots, w_n)^T$$

In the formula:  $W$  ——eigenvector;  $w_i$  ——the value of  $i$ -th row in  $w, i = 1, 2, \dots, n$

4) Calculation of the eigenvalue  $\lambda_{\max}$

$$\lambda_{\max} = \sum_{i=1}^n \frac{(Aw)_i}{nw_i}$$

In the formula:

$\lambda_{\max}$  —— maximum eigenvalue  $w_i$  —— eigenvector;  $A$  —— judgment matrix.

### 3.3. 3. Data Source and Application

Taking the three-level index T1-T68 in Table.3 in this paper as content, the questionnaire of sorting the importance of the audit index system was set up, 36 questionnaires are distributed to the audit bureau, design institute, project management company and relevant professional teachers in colleges and universities, and people with practical experience through the WJX APP, and 31 valid questionnaires were recovered. The above-mentioned FAHP model is used to calculate the weight of each index.

(1) Building of judgment matrix

This paper selects the No. 5 expert questionnaire to compare the information in two layers, assigns values to each index factor, and obtains the judgment matrix of each level, the comparison logic of the hierarchy of the judgment matrix  $P_1—P_3, S_1—S_9, S_{10}—S_{18}, S_{19}—S_{23}, T_1—T_2, T_3—T_6, T_7—T_{11}, T_{16}—T_{18}, T_{19}—T_{21}, T_{22}—T_{25,26}—T_{28}, T_{29}—T_{30}, T_{31}—T_{33}, T_{34}—T_{36}, T_{37}—T_{40}, T_{41}—T_{42}, T_{43}—T_{45}, T_{46}—T_{47}, T_{48}—T_{50}, T_{51}—T_{52}, T_{53}—T_{55}, T_{56}—T_{58}, T_{59}—T_{60,61}—T_{62}, T_{63}—T_{64}, T_{65}—T_{68}$ . Due to a large number of judgment matrices and a large amount of data, this paper extracts some matrices for display, as shown in Table.4-9:



**Table 4.** P1-P3 index judgment matrix

P	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>
P <sub>1</sub>	1	9	4.5
P <sub>2</sub>	0.11	1	0.22
P <sub>3</sub>	0.22	4.5	1

**Table 5.** S1-S9 index judgment matrix

S <sub>1-9</sub>	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>	S <sub>5</sub>	S <sub>6</sub>	S <sub>7</sub>	S <sub>8</sub>	S <sub>9</sub>
S <sub>1</sub>	1	3.375	4.5	9	2.25	7.875	1.125	6.75	5.625
S <sub>2</sub>	0.296	1	1.125	5.625	0.889	4.5	0.444	3.375	2.25
S <sub>3</sub>	0.222	0.889	1	4.5	0.444	3.375	0.296	2.25	1.125
S <sub>4</sub>	0.11	0.178	0.222	1	0.148	0.889	0.127	0.444	0.296
S <sub>5</sub>	0.444	1.125	2.25	6.75	1	5.625	0.889	4.5	3.375
S <sub>6</sub>	0.127	0.222	0.296	1.125	0.178	1	0.148	0.889	0.444
S <sub>7</sub>	0.889	2.25	3.375	7.875	1.125	6.75	1	5.625	4.5
S <sub>8</sub>	0.148	0.296	0.444	2.25	0.222	1.125	0.178	1	0.889
S <sub>9</sub>	0.178	0.444	0.889	3.375	0.296	2.25	0.222	1.125	1

**Table 6.** T1-T2 index judgment matrix

T <sub>1-2</sub>	T <sub>1</sub>	T <sub>2</sub>
T <sub>1</sub>	1	9
T <sub>2</sub>	0.11	1

**Table 7.** T3-T6 index judgment matrix

T <sub>3-6</sub>	T <sub>3</sub>	T <sub>4</sub>	T <sub>5</sub>	T <sub>6</sub>
T <sub>3</sub>	1	9	3	6
T <sub>4</sub>	0.11	1	0.167	0.333
T <sub>5</sub>	0.333	6	1	3
T <sub>6</sub>	0.167	3	0.333	1

**Table 8.** T63-T64 index judgment matrix

T <sub>63-64</sub>	T <sub>63</sub>	T <sub>64</sub>
T <sub>63</sub>	1	9
T <sub>64</sub>	0.11	1

**Table 9.** T65-T68 index judgment matrix

T <sub>65-68</sub>	T <sub>65</sub>	T <sub>66</sub>	T <sub>67</sub>	T <sub>68</sub>
T <sub>65</sub>	1	9	3	6
T <sub>66</sub>	0.11	1	0.167	0.333
T <sub>67</sub>	0.333	6	1	3
T <sub>68</sub>	0.167	3	0.333	1

(2) Calculation of index weight

According to the corresponding judgment matrix sorted out, MATLAB program is used to solve the weight vector and maximum eigenvalue of each judgment matrix, on the basis of the information of the No.5 expert questionnaire, the weight of each audit index calculated to the importance of the whole index system is obtained, for details, see the data of "Expert No.5" in Table.10.

(3) Calculation of the overall average index weight

3. data source was adopted and (1) and (2) steps were applied, 31 valid questionnaires were analyzed and calculated, respectively, and then the corresponding index weights were averaged, and finally the average weight of each index relative to the importance of the whole index system was obtained, for details, see the "average" data in Table.10.

**Table 10.** The calculation results of whole-process tracking audit index system weight of "special bonds + PPP"

first-level index	index weight		second-level index	index weight		third-level index	index weight	
	No.5 expert	average		No.5 expert	average		No.5 expert	average
P <sub>1</sub>	0.7276	0.4879	S <sub>1</sub>	(0.2864)0.2084	0.1705)0.0832	T <sub>1</sub>	(0.9000) 0.1876	(0.5129) 0.0427
						T <sub>2</sub>	(0.1000) 0.0208	(0.4871) 0.0405
						T <sub>3</sub>	(0.5913) 0.0485	(0.235) 0.0145
			S <sub>2</sub>	(0.1127)0.0820	(0.1265)0.0617	T <sub>4</sub>	(0.0465) 0.0038	(0.2324) 0.0143
						T <sub>5</sub>	(0.2570) 0.0211	(0.2713) 0.0167
						T <sub>6</sub>	(0.1052) 0.0086	(0.2613) 0.0162
			S <sub>3</sub>	(0.0789)0.0574	(0.1189)0.058	T <sub>7</sub>	(0.0378) 0.0022	(0.1727) 0.01
						T <sub>8</sub>	(0.4928) 0.0283	(0.2145) 0.0124
						T <sub>9</sub>	(0.2662) 0.0153	(0.2149) 0.0125
			S <sub>4</sub>	(0.0220)0.0160	(0.0819)0.0399	T <sub>10</sub>	(0.1352) 0.0077	(0.1707) 0.0099
						T <sub>11</sub>	(0.0680) 0.0039	(0.2272) 0.0132
						T <sub>12</sub>	(0.5913) 0.0095	(0.2917) 0.0116
						T <sub>13</sub>	(0.1052) 0.0017	(0.2517) 0.0100
						T <sub>14</sub>	(0.2570) 0.0041	(0.2312) 0.0093
			T <sub>15</sub>	(0.0465) 0.0007	(0.2254) 0.0090			

			T <sub>16</sub>	(0.7276) 0.0841	(0.3461) 0.0130
			T <sub>17</sub>	(0.2112) 0.0244	(0.3891) 0.0146
S <sub>5</sub>	(0.1589)0.1156	(0.0771)0.0376	T <sub>18</sub>	(0.0613) 0.0071	(0.2648) 0.0100
			T <sub>19</sub>	(0.0613) 0.0013	(0.3246) 0.0178
			T <sub>20</sub>	(0.7276) 0.0149	(0.3031) 0.0166
S <sub>6</sub>	(0.0282)0.0205	(0.1123)0.0548	T <sub>21</sub>	(0.2112) 0.0043	(0.3723) 0.0204
			T <sub>22</sub>	(0.2570) 0.0410	(0.2517) 0.0106
			T <sub>23</sub>	(0.5913) 0.0943	(0.2498) 0.0105
S <sub>7</sub>	(0.2191)0.1594	(0.0863)0.0421	T <sub>24</sub>	(0.1052) 0.0167	(0.2615) 0.0110
			T <sub>25</sub>	(0.0465) 0.0074	(0.2371) 0.0100
			T <sub>26</sub>	(0.7276) 0.0205	(0.3842) 0.0251
			T <sub>27</sub>	(0.2112) 0.0060	(0.3175) 0.0207
S <sub>8</sub>	(0.0387)0.0282	(0.1337)0.0653	T <sub>28</sub>	(0.0613) 0.0017	(0.2983) 0.0195
			T <sub>29</sub>	(0.1000) 0.0040	(0.4613) 0.0209
S <sub>9</sub>	(0.0551)0.0401	(0.0928)0.0453	T <sub>30</sub>	(0.9000) 0.0361	(0.5387) 0.0244
			T <sub>31</sub>	(0.0613) 0.0011	(0.3676) 0.0203
			T <sub>32</sub>	(0.7276) 0.0128	(0.3246) 0.0179
S <sub>10</sub>	(0.2863)0.0176	(0.1814)0.0553	T <sub>33</sub>	(0.2112) 0.0037	(0.3078) 0.0170
			T <sub>34</sub>	(0.2112) 0.0015	(0.3079) 0.0095
			T <sub>35</sub>	(0.7276) 0.0050	(0.3197) 0.0098
S <sub>11</sub>	(0.1127) 0.0069	(0.1011) 0.0308	T <sub>36</sub>	(0.0613) 0.0004	(0.3724) 0.0115
			T <sub>37</sub>	(0.2570) 0.0025	(0.2575) 0.0100
			T <sub>38</sub>	(0.5913) 0.0057	(0.2578) 0.0100
S <sub>12</sub>	(0.1589) 0.0097	(0.1278) 0.0389	T <sub>39</sub>	(0.1052) 0.0010	(0.2517) 0.0098
P <sub>2</sub>	0.0613	0.3046	T <sub>40</sub>	(0.0465) 0.0005	(0.2331) 0.0091
			T <sub>41</sub>	(0.9000) 0.0122	(0.5645) 0.0237
S <sub>13</sub>	(0.2190)0.0135	(0.1379) 0.042	T <sub>42</sub>	(0.1000) 0.0013	(0.4355) 0.0183
			T <sub>43</sub>	(0.7276) 0.0009	(0.3198) 0.0101
			T <sub>44</sub>	(0.2112) 0.0003	(0.3342) 0.0105
S <sub>14</sub>	(0.0220) 0.0013	(0.1033) 0.0315	T <sub>45</sub>	(0.0613) 0.0001	(0.3461) 0.0109
			T <sub>46</sub>	(0.1000) 0.0002	(0.5645) 0.0110
S <sub>15</sub>	(0.0387) 0.0024	(0.0641) 0.0195	T <sub>47</sub>	(0.9000) 0.0022	(0.4355) 0.0085
			T <sub>48</sub>	(0.2112) 0.0004	(0.4057) 0.0119
S <sub>16</sub>	(0.0284) 0.0017	(0.0964) 0.0294			

				T <sub>49</sub>	(0.7276) 0.0012	(0.2795) 0.0082
				T <sub>50</sub>	(0.0613) 0.0001	(0.3148) 0.0093
			S <sub>17</sub>	(0.0789) 0.0048	(0.0649) 0.0197	T <sub>51</sub> (0.1000) 0.0005 (0.5903) 0.0116
						T <sub>52</sub> (0.9000) 0.0043 (0.4097) 0.0081
			S <sub>18</sub>	(0.0551) 0.0034	(0.1231) 0.0375	T <sub>53</sub> (0.0613) 0.0002 (0.3343) 0.0125
						T <sub>54</sub> (0.7276) 0.0025 (0.4009) 0.0150
						T <sub>55</sub> (0.2112) 0.0007 (0.2648) 0.0099
			S <sub>19</sub>	(0.1352) 0.0285	(0.2187) 0.0454	T <sub>56</sub> (0.0613) 0.0017 (0.2053) 0.0093
						T <sub>57</sub> (0.7276) 0.0207 (0.3294) 0.0150
						T <sub>58</sub> (0.2112) 0.0061 (0.4653) 0.0211
			S <sub>20</sub>	(0.2662) 0.0562	(0.2317)0.0482	T <sub>59</sub> (0.9000) 0.0506 (0.5645) 0.0272
						T <sub>60</sub> (0.1000) 0.0056 (0.4355) 0.0210
P <sub>3</sub>	0.2111	0.2075	S <sub>21</sub>	(0.4928) 0.1040	(0.2398) 0.0496	T <sub>61</sub> (0.1000) 0.0104 (0.6677) 0.0331
						T <sub>62</sub> (0.9000) 0.0936 (0.3323) 0.0165
			S <sub>22</sub>	(0.0680) 0.0144	(0.1727) 0.0358	T <sub>63</sub> (0.1000) 0.0014 (0.6161) 0.0221
						T <sub>64</sub> (0.9000) 0.0130 (0.3839) 0.0137
						T <sub>65</sub> (0.2570) 0.0021 (0.2664) 0.0076
			S <sub>23</sub>	(0.0378) 0.0080	(0.1371) 0.0285	T <sub>66</sub> (0.5913) 0.0047 (0.2750) 0.0078
						T <sub>67</sub> (0.1052) 0.0008 (0.2233) 0.0064
						T <sub>68</sub> (0.0465) 0.0004 (0.2353) 0.0067

Note: there are weights for the upper-level indexes in bracket, and there are weights for the whole index system outside the bracket.

#### 4. Conclusion

(1) Through literature research and interviews with institutional experts, the reasonable dimensions and important content identification of the whole-process tracking audit of "special bonds + PPP" were analyzed, according to the three dimensions: early project approval decision, middle-term administration, and later handover evaluation, the evaluation index system including 3 first-level indexes, 23 second-level indexes and 68 third-level indexes were built, the audit work covered the whole life cycle of the project, and ensured the legal operation of the project and achieve the expected benefits.

(2) The questionnaire information is based on the importance sorting of the evaluation index system filled in by experts, in order to avoid the shortcomings of the traditional AHP, namely, there are many indexes in this paper, and it is difficult to determine the weight of each index by "comparison in pairs", so the FAHP is introduced, the factor sorting and assignment are made to each index, the judgment matrix is built, and MATLAB program is used to obtain the mean value of weight, which makes the audit index system scientific and operable.

This paper focused on the building contents of the whole-process tracking audit index system of "special bonds + PPP" and the weight of each index, and made the audit work well-founded.

In the future research, we will further study the audit prediction model matching this index system, and provide theoretical and practical support for the project audit activities of government departments.

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## References

- [1] Yan Xiaojian. Application and Audit Focus of Public-Private Partnership (PPP)[J]. Auditing Research, 2014(05):45-51.
- [2] Lu Xinyi. Audit of Public-Private Partnerships (PPP) in Infrastructure Projects in India and Its Applications[J]. Auditing Research, 2015(04):55-59
- [3] Shi Xian. Auditing the State Construction Projects under the Model Public-Private Partnership[J]. Audit Economy Research, 2016, 31(03): 3-9.
- [4] Wang Ligu, Zhang Ying. Discussion on PPP Project Tracking Audit[J]. Auditing Research, 2016(06):30-35.
- [5] Fang Jun, Ren Suping, Huang Juntian. Design of Evaluation Indicator System for Whole-Process Real-Time Audit of PPP Projects[J]. Auditing Research, 2017(06): 14-21+98.
- [6] Zhao Chong, Gao Yun, Ji Lei, Guo Shurong. Research on the Tracking Audit of PPP Projects Based on the Whole Life Cycle [J]. Accountant, 2017(13):57-58.
- [7] Ye Xiaosu, Zhang Deqin, Shi Shiyong. Research on the Construction of Audit Mechanism in PPP Project[J]. Construction Economy, 2017, 38(08): 49-54.
- [8] Huang Wanyi, Lu Yongsong. Analysis on the Multi-Dimensional Tracking Audit of the Whole Process of PPP Projects[J]. Cities and Towns Construction in Guangxi, 2020(09):86-88.
- [9] Sun Lingzhi, Jia Hongjun, Ren Yixin. Study on the Characteristics, Mechanisms and Approaches of Audit Supervision in PPP-model Construction Projects[J]. Auditing Research, 2016(02):44-49.
- [10] Jiao Sheng. Influence of PPP Mode on Construction Project Audit and Path Optimization [J]. Commercial Accounting, 2017(05):36-39.
- [11] Wen Laicheng, Diao Weitao, Chen Baodong, Ruan Jing. Prevent Risks and Improve Benefit, and Strengthen Administration of Special Bonds[J]. Caizheng Jiandu, 2020(22):23-29.
- [12] Chai Yunlong. Application and Control of Financing Ways of Governmental Special Bonds [J]. China Market, 2020(33): 28-29.
- [13] Xu Bo, Yang Wei. Analysis of the Risk Points of Local Government Special Bonds [J]. Fiscal Science, 2020(06): 77-85.